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## **Topics**

### **Exponents**

1. Basic Rules
2. Fractional Exponents
3. Simplifying Radicals

### **Factoring**

4. Factoring by GCF
5. Factoring quadratic expressions
6. Special Factoring formulas
7. Factoring through synthetic division

### **Equations/Inequalities**

8. Solving linear equations.
9. Solving quadratic equations by factoring
10. Solving quadratic equations by quadratic formula
11. Solving radical equations
12. Solving rational equations
13. Solving logarithmic equations

### **Functions**

14. Function notation
15. Function names
16. Function Operations.

### **Graphing**

17. Function transformations
18. Graphing Parent Functions by T-chart using “smart” points
19. Basic Graphing using “smart” points

### **General Topics**

20. Distance and Midpoint formulas
21. Intercepts
22. Equations of lines
23. Pythagorean Theorem
24. Common Algebraic Errors

Name \_\_\_\_\_

**1: Exponent Rules**

Simplify the following

1.  $(-2^2)^3$       2.  $-\left(\frac{2}{5}\right)^{-2}$       3.  $(3x^2y)^{-3}$

4.  $\frac{y^{-4}}{5x^{-2}}$       5.  $\frac{x^{-1}y}{xy^{-2}}$       6.  $\frac{3xy^9}{2y^{-2}} \cdot \frac{-7y}{42x^5}$

**2: Fractional Exponents**

Evaluate the following without a calculator

1.  $8^{\frac{2}{3}}$       2.  $4^{-\frac{1}{2}}$       3.  $(\sqrt[4]{16})^2$

4.  $\sqrt[3]{1000^2}$       5.  $(\sqrt[3]{-27})^4$       6.  $-(25^{-\frac{3}{2}})$

**3: Simplifying Radicals**

Simplify and rationalize the following.

1.  $\sqrt{80}$       2.  $\sqrt[4]{32}$       3.  $\sqrt[3]{54x^3}$

4.  $\frac{3}{\sqrt{8}}$       5.  $\sqrt{\frac{4}{75}}$       6.  $4\sqrt{3} \cdot \sqrt{21}$

**4: Factoring by GCF**

Factor the following completely

1.  $3x^4 - 9x^2$

2.  $49xy + 28x - 14y$

3.  $18x^3y^5 - 12x^4y^2$

**5: Factoring Quadratic Expressions**

Factor the following completely

1.  $x^2 - 3x + 2$

2.  $x^2 + 5x - 6$

3.  $2x^2 + 5x - 3$

4.  $3x^2 - 8x + 4$

5.  $3x^2 + 17x + 10$

6.  $10x^2 - 19x + 6$

**6: Special Factoring**

$$a^2 + 2ab + b^2 = (a+b)^2 \quad a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$a^2 - 2ab + b^2 = (a-b)^2 \quad a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$a^2 - b^2 = (a+b)(a-b)$$

Factor the following completely

1.  $4x^2 - 20x + 25$

2.  $49x^2 + 42xy + 9y^2$

3.  $16x^4 - 81$

4.  $x^3 - 8$

5.  $125x^3 + y^3$

6.  $64 - 27y^6$

## 7: Factoring through Synthetic Division

Use synthetic division to factor as indicated.

1.  $x^3 - 4x^2 + 2x + 1 = (x - 1)(\quad)$

2.  $2x^3 + 5x + 7 = (x + 1)(\quad)$

3.  $x^4 - 3x^3 + x^2 + x + 2 = (x - 2)(\quad)$

4.  $4x^4 + 3x^2 - 1 = (2x - 1)(\quad)$

## 8: Solving Linear Equations

Solve the following for the unknown variable.

1.  $\frac{2x+1}{5} = \frac{3x+1}{2}$

2.  $\frac{x}{2} + \frac{5x}{6} = \frac{2x}{3} + \frac{1}{12}$

3.  $3(x - 8) + 4x = 5x - (x + 7)$

## 9: Solving Quadratic Equations by Factoring

Factor to solve for x.

1.  $x^2 + 5x + 6 = 0$

2.  $8x^2 - 6x - 5 = 0$

3.  $11x^2 - 14x - 16 = 0$

**10: Solving Quadratic Equations using the Quadratic Formula**

For each equation, solve for the indicated expression.

1.  $2x^2 - 4x - 1 = 0 \text{ for } x$

2.  $2x^2 + 2x + 3 = 0 \text{ for } x$

3.  $x^4 - 4x^2 + 2 = 0 \text{ for } x^2$

**11: Solving Radical Equations**

Solve the following for x.

1.  $\sqrt{x} = 3x - 1$

2.  $3\sqrt{2x} + 1 = 7$

3.  $3x^{\frac{3}{4}} - 5 = 19$

**12: Solving Rational Equations**

Solve the following for x

1.  $\frac{3}{2x} - \frac{9}{2} = 6x$

2.  $\frac{2}{3x} + \frac{2}{3} = \frac{8}{x+6}$

3.  $\frac{2}{x+1} + \frac{x}{x-1} = \frac{2}{x^2-1}$

**13: Solving Logarithmic Equations**

Solve the following for x

1.  $\log_3 3^x = 7$

2.  $\log_9 x = \frac{1}{2}$

3.  $2 \log_3(x+1) = 4$

#### 14: Function Notation

Given  $f(x) = -x^2 + x$ , answer the following questions.

1. Find  $f(0)$

2. Find  $f(x) = 0$

3. Find  $f\left(-\frac{1}{3}\right)$

Given  $f(x) = \frac{1}{3}x + \frac{7}{4}$ , answer the following questions.

4. Find the zeros of  $f(x)$

5. Solve  $f(x) = \frac{1}{8}$

6. Find  $f\left(-\frac{9}{8}\right)$

#### 15: Function Names

Match the following equations to their description.

- |          |   |                            |
|----------|---|----------------------------|
| _____ 1. | $f(x) = \frac{2}{3} 4x+5  - 3$                | A. Linear Function         |
| _____ 2. | $f(x) = \frac{2}{3}\sqrt[3]{4x+5} - 3$        | B. Quadratic Function      |
| _____ 3. | $f(x) = \frac{2}{3} \cdot \frac{1}{4x+5} - 3$ | C. Absolute Value Function |
| _____ 4. | $f(x) = \frac{2}{3}(4x+5)^4 - 3(4x+5)^2 - 2$  | D. Cubic Function          |
| _____ 5. | $f(x) = \frac{2}{3}(4x+5)^3 - 3$              | E. Cube Root Function      |
| _____ 6. | $f(x) = \frac{2}{3}(4x+5) - 3$                | F. Square Root Function    |
| _____ 7. | $f(x) = \frac{2}{3}(4x+5)^2 - 3$              | G. Rational Function       |
| _____ 8. | $f(x) = \frac{2}{3}\sqrt{4x+5} - 3$           | H. Polynomial Function     |

## 16: Function Operations

Perform the following function operations if  $f(x) = 2x^2$  and  $g(x) = 3 - 4x$

1.  $f(g(x))$

2.  $g(f(x))$

3.  $(f - g)(x)$

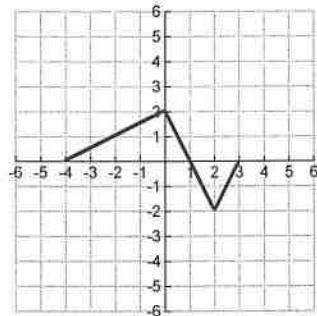
4.  $f(f(x))$

5.  $g(g(x))$

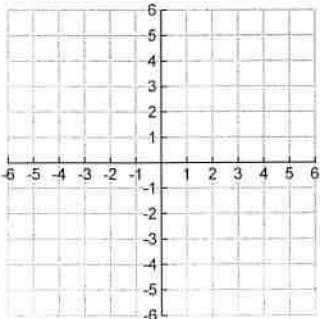
6. Find  $g(g(x)) = 0$

## 17: Function Transformation

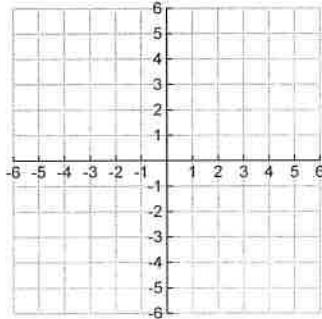
Use the graph of  $y = f(x)$  at the right to sketch the following transformations.



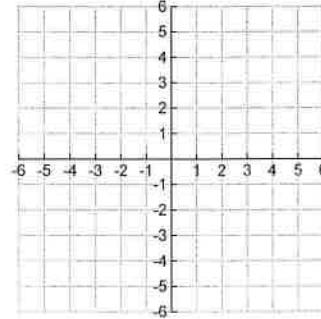
1.  $y = 2f(x)$



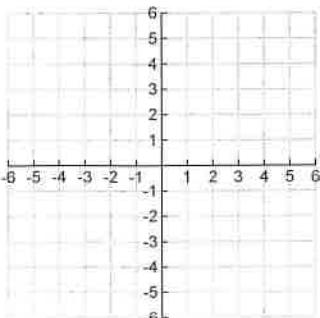
2.  $y = -f(x)$



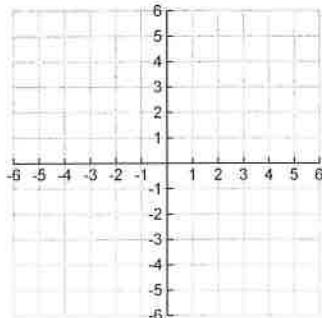
3.  $y = f(x-1)$



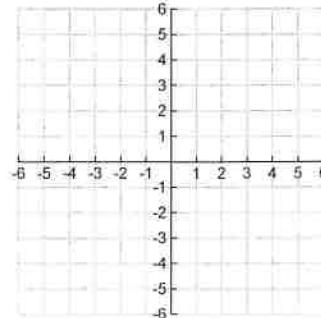
4.  $y = f(x)+2$



5.  $y = f(-x)$



6.  $y = -2f(x+2)+1$



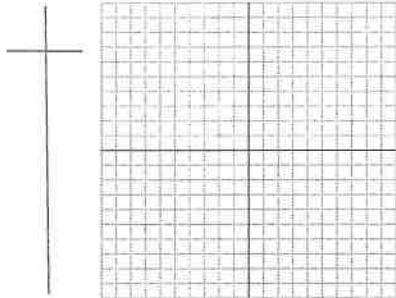
## 18: Graphing Parent Functions using T-Charts

Graph the following using a T-Chart with “smart” values. State the Domain and Range of each function.

1.  $f(x) = x^2$

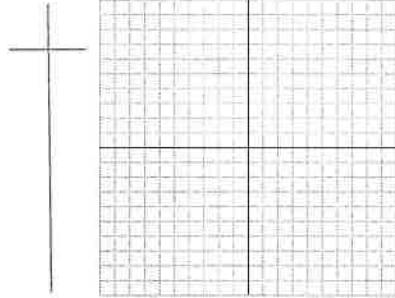
2.  $f(x) = \sqrt{x}$

3.  $f(x) = |x|$



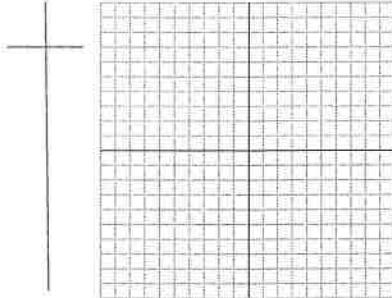
D:

R:



D:

R:



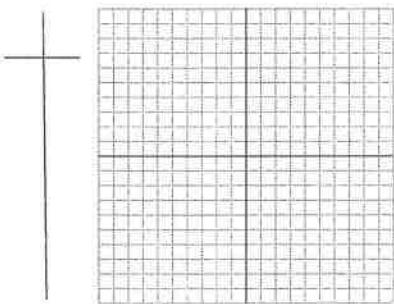
D:

R:

4.  $f(x) = x^3$

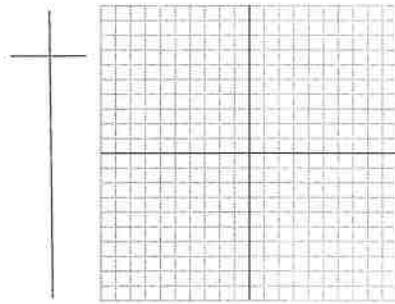
5.  $f(x) = \sqrt[3]{x}$

6.  $f(x) = \frac{1}{x}$



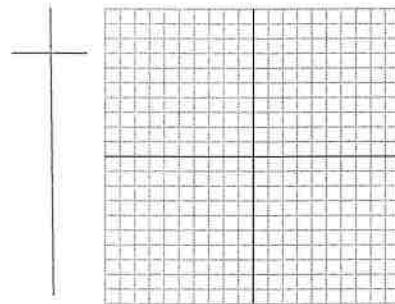
D:

R:



D:

R:



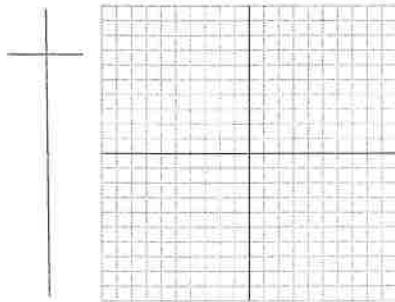
D:

R:

7.  $f(x) = x$

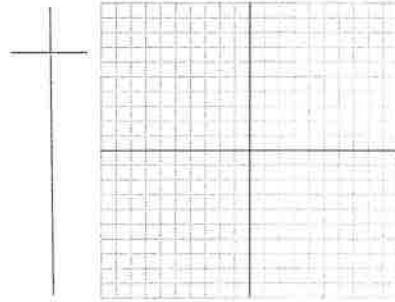
8.  $f(x) = 2^x$

9.  $f(x) = \log_2 x$



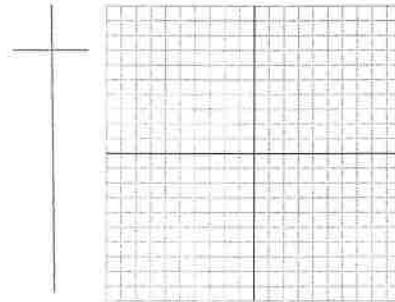
D:

R:



D:

R:



D:

R:

### 19: Basic Graphing Choosing “Smart” Points

Fill in the T-chart using at least 3 smart x-values (that enable you to find exact points)

1.  $f(x) = \sqrt{3-x}$



2.  $f(x) = \frac{7}{x-2}$



3.  $f(x) = 3^{\frac{x}{4}}$



### 20: Distance and Midpoint Formulas

Find the distance between the two points. Then find the midpoint between the two points.

1.  $(-2, 5); (6, -1)$

2.  $\left(\frac{3}{2}, -\frac{1}{2}\right); \left(-\frac{3}{2}, \frac{7}{2}\right)$

3.  $\left(\frac{5}{2}, -\frac{3}{2}\right); (1, -4)$

### 21: Intercepts

Use the following equations to find the x and y intercept(s)

1.  $y^2 = x + 9$

2.  $9x^2 + 4y^2 = 36$

3.  $\left(\frac{x+4}{2}\right)^2 + y^2 = 1$

### 22: Equations of Lines

Find the equation of the line that has the given characteristics. Leave your answer in the form indicated.

1. slope =  $\frac{3}{4}$ ; y-int :  $-\frac{2}{3}$

(Standard Form)

2. Parallel to  $2x + 3y = 4$  through

$(-3, 6)$

3. Perpendicular to  $4x - 7y = 23$

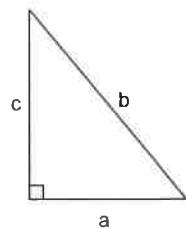
through  $\left(\frac{2}{3}, -\frac{4}{5}\right)$

(Slope-intercept form)

(Point-Slope Form)

### 23: Pythagorean Theorem

Use the diagram at the right to answer the following questions. Be sure to simplify.



1. Find  $b$  if  $a = 4\sqrt{5}$ ,  $c = 2$

2. Find  $c$  if  $a = 2\sqrt{3}$ ,  $b = 6$

3. If  $a = c$ , and  $b = 10$ , find  $a$

### 24: Algebraic Errors to Avoid

Error	Correct form	Comments
$a - (x - b) \neq a - x - b$	$a - (x - b) = a - x + b$	Change all signs when distribution negative through parentheses.
$(a + b)^2 \neq a^2 + b^2$	$(a + b)^2 = a^2 + 2ab + b^2$	Don't forget middle term when squaring binomials.
$\left(\frac{1}{2}a\right)\left(\frac{1}{2}b\right) \neq \frac{1}{2}ab$	$\left(\frac{1}{2}a\right)\left(\frac{1}{2}b\right) = \frac{1}{4}(ab)$	$\frac{1}{2}$ occurs twice as a factor.
$\frac{a}{x + b} \neq \frac{a}{x} + \frac{a}{b}$	Leave as $\frac{a}{x + b}$	Don't add denominators when adding fractions.
$\frac{1}{a} + \frac{1}{b} \neq \frac{1}{a + b}$	$\frac{1}{a} + \frac{1}{b} = \frac{a + b}{ab}$	Use definition for adding fractions.
$\frac{x}{a} \neq \frac{bx}{a}$	$\frac{x}{a} = \left(\frac{x}{a}\right)\left(\frac{1}{b}\right) = \frac{x}{ab}$	Multiply by reciprocal of the denominator.
$\frac{1}{3x} \neq \frac{1}{3}x$	$\frac{1}{3x} = \frac{1}{3} \cdot \frac{1}{x}$	Use definition for multiplying fractions.
$1/x + 2 \neq \frac{1}{x + 2}$	$1/x + 2 = \frac{1}{x} + 2$	Be careful when using a slash to denote division.
$(x^2)^3 \neq x^5$	$(x^2)^3 = x^{2 \cdot 3} = x^6$	Multiply exponents when an exponential form is raised to a power.
$2x^3 \neq (2x)^3$	$2x^3 = 2(x^3)$	Exponents have priority over coefficients.
$\frac{1}{x^2 + x^3} \neq x^{-2} + x^{-3}$	Leave as $\frac{1}{x^2 + x^3}$	Don't shift term-by-term from denominator to numerator.
$\sqrt{5x} \neq 5\sqrt{x}$	$\sqrt{5x} = \sqrt{5}\sqrt{x}$	Radicals apply to every factor inside radical.
$\sqrt{x^2 + a^2} \neq x + a$	Leave as $\sqrt{x^2 + a^2}$	Don't apply radicals term-by-term.
$\frac{a + bx}{a} \neq 1 + bx$	$\frac{a + bx}{a} = 1 + \frac{b}{a}x$	Cancel common factor, <i>not</i> common terms.
$\frac{a + ax}{a} \neq a + x$	$\frac{a + ax}{a} = 1 + x$	Factor <i>before</i> canceling.

Multiplying Polynomials  
No Calculator!!!

1.  $(x + 7)^2$

2)  $(x - 11)^2$

3.  $(x + 4)^3$

4.  $(x + h)^3$

5.  $(x + 1)(x^2 - 3x - 4)$

6.  $(x + h)(x^2 + 3xh + 8)$

7.  $(a + b)^2$

Factoring  
No Calculator!!

Factor each polynomial completely. If the polynomial cannot be factored write prime.

1)  $2x^2 - 128$

2)  $x^2 - 10x + 24$

3)  $a^3 - 64b^3$

4)  $5x^2 + 40x - 10$

5)  $2x^2 - 11x + 12$

6)  $x^3 + 16x^2 + 64x$

7)  $x^3 + 3x^2 - 4x - 12$

8)  $24x^2 - 54$

9)  $6x^3 - 18x^2$

10)  $5c^2 + 4cd - d^2$

11)  $27y^3 + 125$

12)  $20x^2 - 4x - 72$

13)  $-x^2 + 100$

14)  $4x^4 - 64$

15)  $a^4 - 2a^2 + 1$

16)  $9x^3 + 12x^2 - 45x$

17)  $n^2 - 2n - np + 2p$

18)  $24x^2 + 4x - 60$

Adding and Subtracting Fractions  
No Calculator!!!

Simplify each expression.

$$1. \frac{2}{3} + \frac{5}{7}$$

$$2. \frac{1}{6} - \frac{5}{18}$$

$$3. \frac{6}{x} + 5$$

$$4. \frac{3x}{4y} - 7$$

$$5. \frac{3}{x^2} - \frac{4}{x}$$

$$6. \frac{x}{x+5} + \frac{7x}{x^2 - 25}$$

$$7. \frac{6}{5x} + \frac{4}{9x} - \frac{1}{3x}$$

$$8. \frac{8}{x^2 - 4x + 4} + \frac{2}{x-2}$$

$$9. \frac{x}{x^2 - 9} + \frac{5}{4x - 12}$$

$$10. \frac{5x}{x-5} + \frac{x+5}{x+2}$$

$$11. \frac{3}{x+3} - \frac{4}{3x}$$

Multiplying and Dividing Fractions  
No Calculator!!!

Simplify each expression.

$$1. \frac{4}{5} \cdot \frac{2}{3}$$

$$2. \frac{1}{9} \cdot -\frac{3}{7}$$

$$3. \frac{\frac{2}{7}}{\frac{4}{9}}$$

$$4. \frac{\frac{11}{7}}{-\frac{7}{18}}$$

$$5. \frac{-\frac{2}{3}}{5}$$

$$6. \frac{\frac{x}{5}}{3}$$

$$7. \frac{4}{13} \cdot \frac{x}{7}$$

$$8. \frac{x+2}{5x} \cdot \frac{-7}{4x}$$

$$9. \frac{11}{10} \cdot 9x$$

$$10. \frac{\frac{8}{3x}}{\frac{5x}{7}}$$

$$11. \frac{\frac{7x+2}{5x-3}}{\frac{9x+4}{6x+7}}$$

$$12. \frac{x}{\frac{2}{5}}$$

$$13. \frac{y}{\frac{z}{7}}$$

$$14. \frac{2 + \frac{3}{7}}{4 - \frac{1}{7}}$$

Remember you cannot cancel at the beginning!!!

$$15. \frac{1 + \frac{1}{x}}{1 - \frac{1}{x}}$$

$$16. \frac{\frac{x-4}{3}}{\frac{x+7}{3}}$$

Rationalize the denominator  
No Calculator!!

$$1) \frac{2}{3-\sqrt{2}}$$

$$2) \frac{\sqrt{7}}{\sqrt{3}+4}$$

$$3) \frac{4+\sqrt{3}}{2-\sqrt{3}}$$

$$4) \frac{2+\sqrt{2}}{6+\sqrt{2}}$$

$$5) \frac{3i-2}{5i-3}$$

$$6) \frac{6-i\sqrt{2}}{6+i\sqrt{2}}$$

$$7) \frac{3+7i}{7i}$$

Solve Quadratic Equations  
No Calculator!!

**Find all real and imaginary solutions for all problems.**

Solve the following by factoring.

$$1) \quad x^2 = 3x + 4$$

$$2) \quad 9x = 10x^2$$

$$3) \quad 8x^2 + 2x = 1$$

$$4) \quad x(x-5) = 36$$

$$5) \quad (x-6)(x-8) = 24$$

Solve the following by using the square root property.

$$6) \quad 3x^2 + 2 = 0$$

$$7) \quad (x+5)^2 - 12 = 0$$

$$8) \quad (2x-5)^2 = -11$$

$$9) \quad 5(4x-3)^2 = 30$$

$$10) \quad \frac{(y+4)^2}{2} = 18$$

Solve the following by completing the square.

$$11) \quad x^2 + 10 = 8x$$

$$12) \quad x^2 - 5x + \frac{41}{4} = 0$$

$$13) \quad 2x^2 + 16x + 39 = 0$$

Solve the following using the Quadratic Formula. You should have the Quadratic Formula memorized.

$$14) \quad 3x^2 = 2 - 9x$$

$$15) \quad 5x^2 - 2x = -4$$

$$16) \quad 12x^2 = x + 6$$

Find the domain of functions

No Calculator!!

State the domain of each function using interval notation.

$$1) \quad f(x) = \sqrt{2x - 5}$$

$$2) \quad f(x) = \frac{x}{5-x}$$

$$3) \quad f(x) = 4x + 5$$

$$4) \quad f(x) = 3x^2 - 4x + 9$$

$$5) \quad f(x) = \frac{x}{x+4}$$

$$6) \quad f(x) = \sqrt{-2x + 5}$$

$$7) \quad f(x) = \frac{1}{3x^2 - 27}$$

$$8) \quad f(x) = \frac{1}{x^2 - 10x + 24}$$

Rational Equations  
No Calculator!!!

Remember the quadratic formula!!!  
Solve each rational equation.

$$1. \frac{x}{x-3} = \frac{2}{5}$$

$$2. 4 = \frac{5}{x} + \frac{2}{3}$$

$$3. \frac{2}{x} + \frac{3x-1}{x+3} = 4$$

$$4. \frac{4x-3}{x-2} = 6 - \frac{x+6}{x+2}$$

$$5. \frac{2}{x+5} + \frac{6}{x^2-25} = \frac{3}{x-5}$$

$$6. \frac{13x+20}{x^2+13x+42} - \frac{4}{x+6} = \frac{6}{x+7}$$

Logarithms  
No Calculator!!!

Write each equation in logarithmic form.

1.  $4^2 = 16$

2.  $5^{-3} = \frac{1}{125}$

Write each equation in exponential form.

3.  $\log_3 81 = 4$

4.  $\log_{49} 7 = \frac{1}{2}$

Evaluate each expression.

5.  $\log 100$

6.  $\log_2 32$

7.  $\log_3 \frac{1}{81}$

8.  $\log_{64} 4$

9.  $\log_5 5^8$

Solve each equation.

10.  $\log_7 x = 3$

11.  $\log_8(5x - 11) = 2$

12.  $\log_x 6 = \frac{1}{2}$

13.  $\log_3 \frac{1}{27} = x$

14.  $\log_4 x + 3 = \log_4(5x^2)$

$$15. \log 125 = 3 \log x$$

$$16. 2 \log_9 3 - \log_9 5 = \log_9 x$$

$$17. \log_4 x + \log_4 2 = 3$$

$$18. \log_3(x+1) - \log_3(x-1) = 4$$